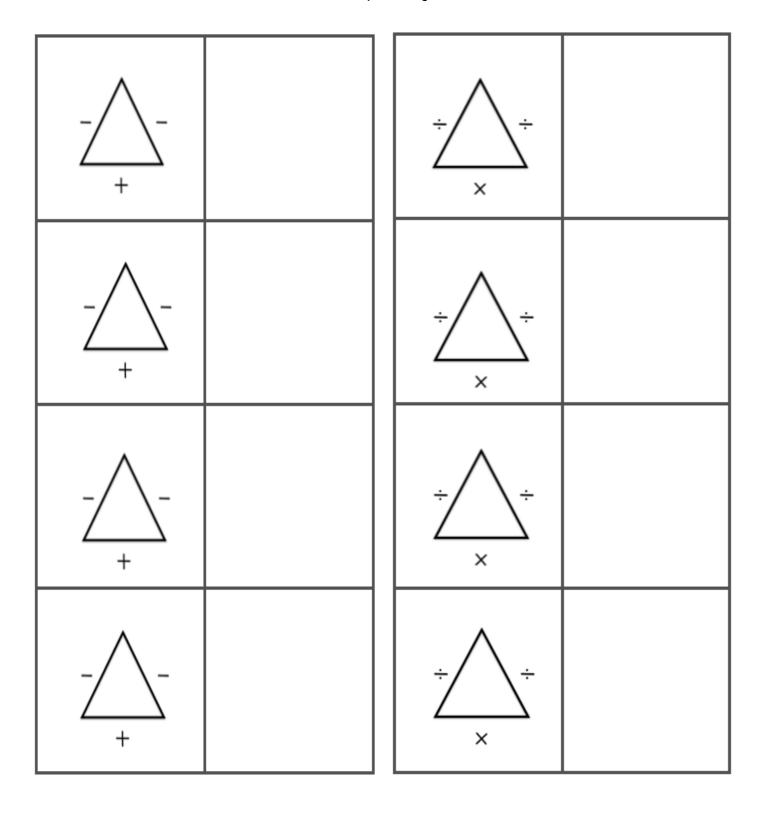
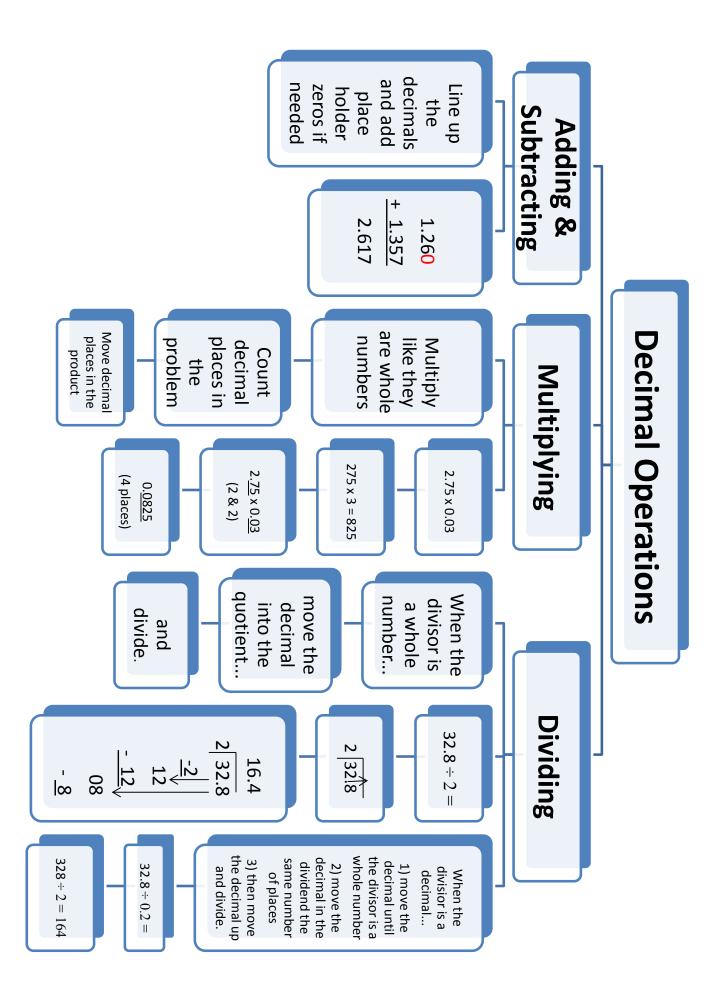
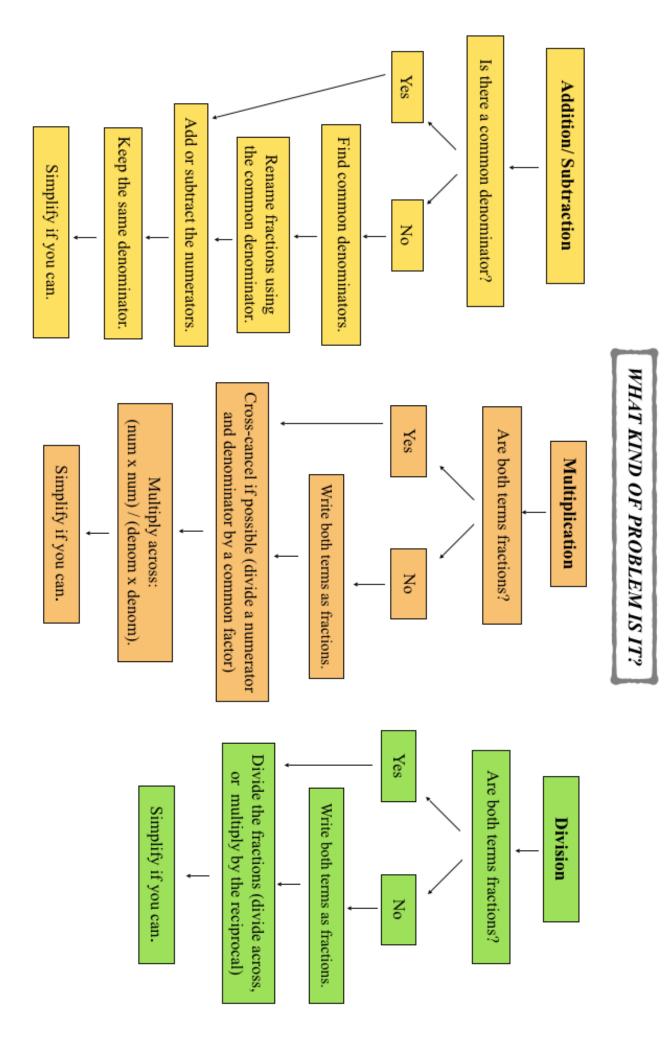
Using Fact Family Triangles to Solve 1-Step Equations



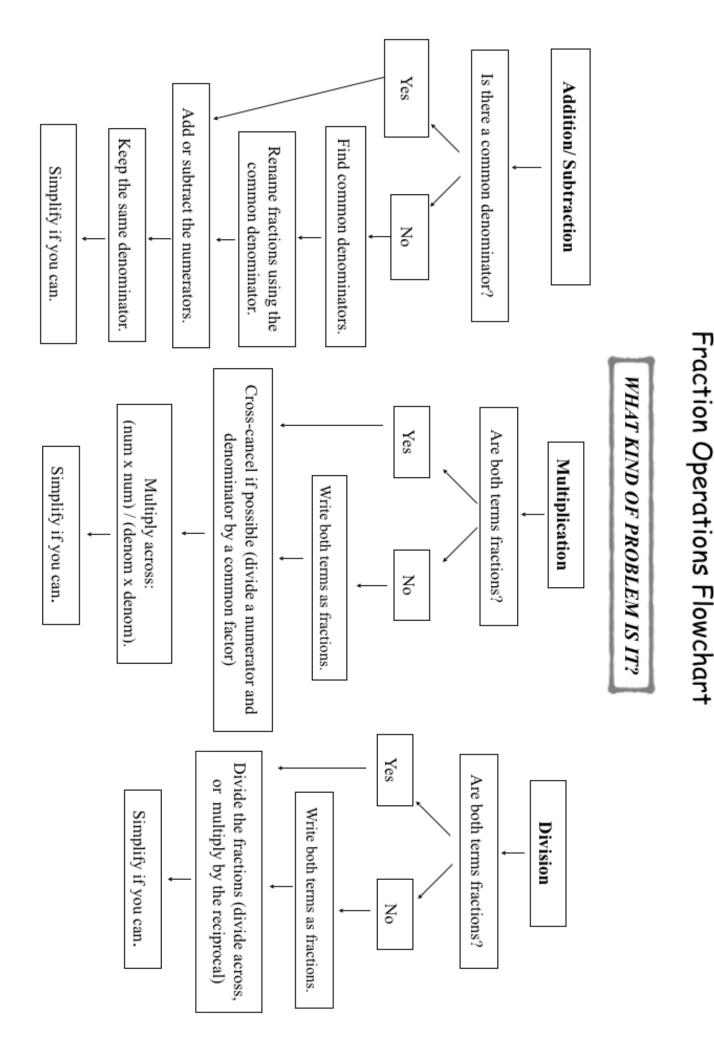
Solving Two Step Equations using Fact Family Triangles
Solving Two Step Equations using Inverse Operations
Solving Two Step Equations Using Diagramming

Strategies for Solving Two Step Equations





Fraction Operations Flowchart



8 + 0.5x = 10.5	-0.03 <i>n</i> – 1.2 = -1.44
-0.6x = 14.4	3.5 ÷ <i>n</i> = 0.07

$n + \frac{4}{5} = \frac{19}{20}$	$\frac{8}{15} - n = \frac{1}{3}$
$\frac{2}{3}x = \frac{7}{10}$	$a \div \frac{1}{4} = \frac{5}{6}$

WORK RECORDING SHEET FOR SCAVENGER HUNT

Show work in the appropriate box. Record the letter that corresponds with your answer.

Show work in the appropriate pox. Record the tetter that corresponds with your answer.		
DECIMAL EQUATIONS: +	DECIMAL EQUATIONS: -	
DECIMAL EQUATIONS: X	DECIMAL EQUATIONS: ÷	
FRACTION EQUATIONS: +	FRACTION EQUATIONS: -	
FRACTION EQUATIONS: X	FRACTION EQUATIONS: ÷	
RATIONAL EQUATIONS: DECIMALS	RATIONAL EQUATIONS: FRACTIONS	

DECIMAL EQUATIONS: +

Solve the equation:		
12.5 + n = 18		
30.5 6.5 5.5		
R	S	Т

DECIMAL EQUATIONS: -

Solve the equation:		
12.5 – n = 10		
2.5 22.5 -2.5		
A E I		

FRACTION EQUATIONS: +

Solve the equation: 2/5 + n = 7/10			
3/5 9/15 3/10			
I O U			

FRACTION EQUATIONS: -

Solve the equation: n - 1/4 = 5/8		
7/8 6/8 3/8		
Y W P		

Solve the equation: 6n = 1.2		
2 0.2 0.02		
D F G		

DECIMAL EQUATIONS: ÷

Solve the equation:			
1.5 ÷ n = 3			
5 4.5 0.5			
H J F			

FRACTION EQUATIONS: x

Solve the equation:		
$\frac{1}{2} \bullet n = \frac{5}{6}$		
5/3 5/12 3/5		
B C D		

FRACTION EQUATIONS: ÷

Solve the equation:		
21 ÷ n = 1/3		
1/63 7 63		
V M B		

RATIONAL EQUATIONS (Decimals)			
Solve the equation:			
0.2n + 1.5 = 3			
0.3 7.5 22.5			
E	B	Μ	

RATIONAL EQUATIONS (Fractions)

Solve the equation: (1/2)n + 4/5 = 9/10			
1/5 1/10 1/20			
!	?	•	



5-9

Solving Equations with Rational Numbers (Pages 244–248)

You can solve rational number equations using the same skills you used to solve equations involving integers.

Solving Equations	 Solving an equation means getting the variable alone on one side of the equation to find its value. To get the variable alone, you use inverse operations to undo what has been done to the variable. Addition and subtraction are inverse operations. Multiplication and division are inverse operations. Whatever you do to one side of the equation, you must also do to the other side to maintain the equality.
----------------------	--

Examples

a. Solve $x + 5.7 = 2.5$.	
x + 5.7 = 2.5	
x + 5.7 - 5.7 = 2.5 - 5.7	Subtract 5.7 from
	each side.
x = -3.2	Simplify.

b. Solve $\frac{2}{3}y = \frac{5}{6}$. $\frac{2}{3}y = \frac{5}{6}$ $\frac{3}{2}\left(\frac{2}{3}y\right) = \frac{3}{2}\left(\frac{5}{6}\right)$ Multiply each side by $\frac{3}{2}$. $y = \frac{5}{4}$ or $1\frac{1}{4}$ Simplify.

Try These Together

1. Solve $\frac{3}{5} = a - \frac{1}{8}$.	2. Solve $1.4n = 4.2$.
HINT: Add $\frac{1}{8}$ to each side.	HINT: Divide each side by 1.4.

Practice

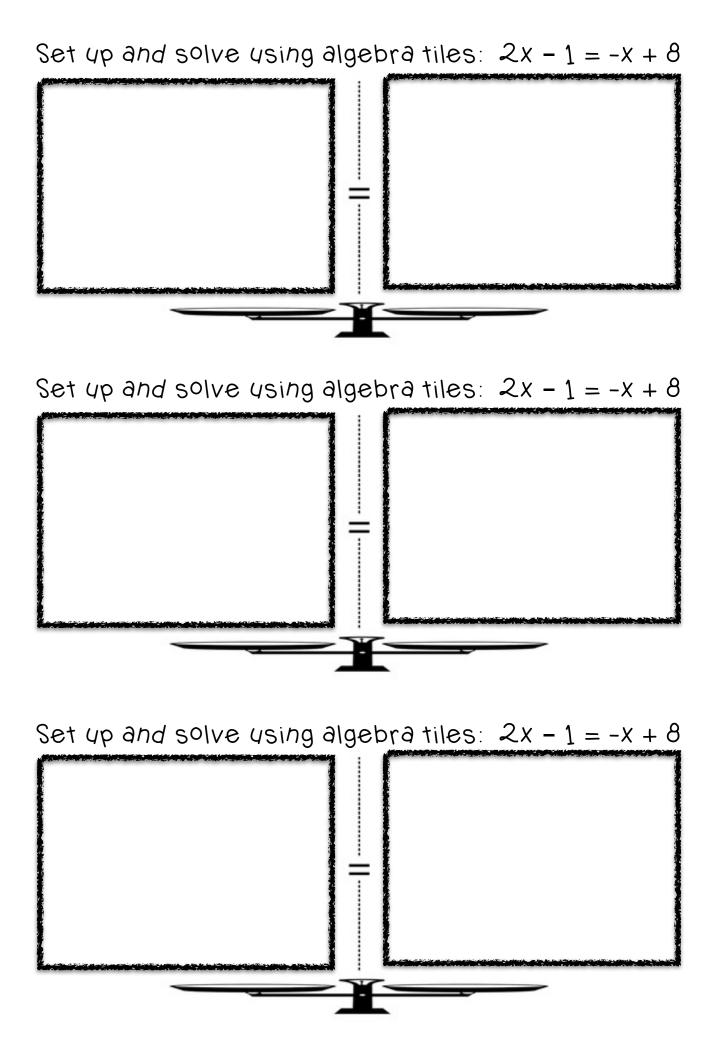
Solve each equation. Check your solution.

3. $p - 3.7 = -2.4$	4. $b - (-60.25) = 121.6$	5. $-8.8 + q = 14.3$
6. $w + \frac{1}{2} = \frac{7}{8}$	7. $j - \left(-\frac{1}{9}\right) = \frac{1}{6}$	8. $y - 1\frac{2}{5} = 2\frac{4}{5}$
9. $-5y = 8.5$	10. $-2.7t = -21.6$	11. $4.2d = -10.5$
12. $9z = \frac{3}{4}$	13. $\frac{m}{5} = -\frac{1}{10}$	14. $-\frac{5}{6}a = 20$
	Solve for the measure of <i>x</i> . 4.4 m 3.4 m	+25.2 m + <i>x</i> + +21.7 m

12'C

Solving Multi-Step Equations

Solving Multi-Step Equations: Combining Like Terms
Solving Multi-Step Equations: Distributive Property
Solving Multi-Step Equations: Simplifying Before Solving



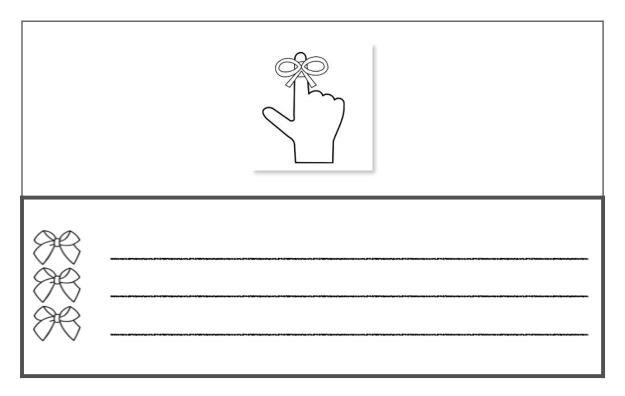
Solving Equations with Variables on Both Sides

2x - 1 = -x + 8	4x - 15 = 17 - 4x	10x - 22 = 29 - 7x

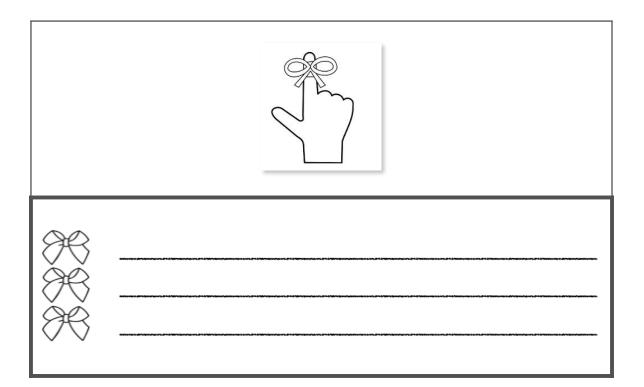
Solving Equations with Variables on Both Sides

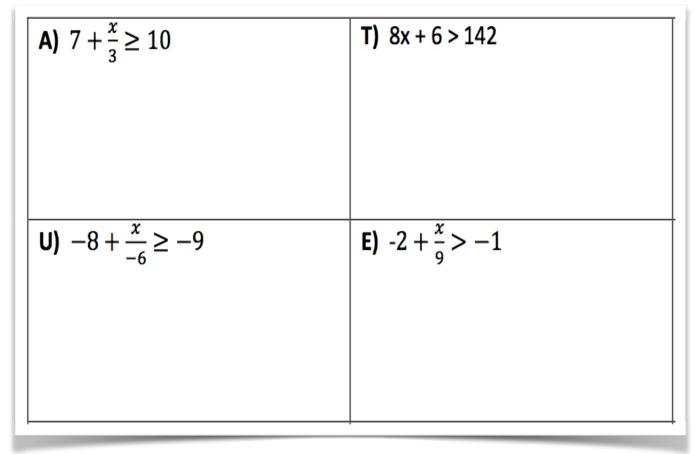
0 • 0		
2x - 1 = -x + 8	4x - 15 = 17 - 4x	10x - 22 = 29 - 7x

Things to Remember!



Things to Remember!





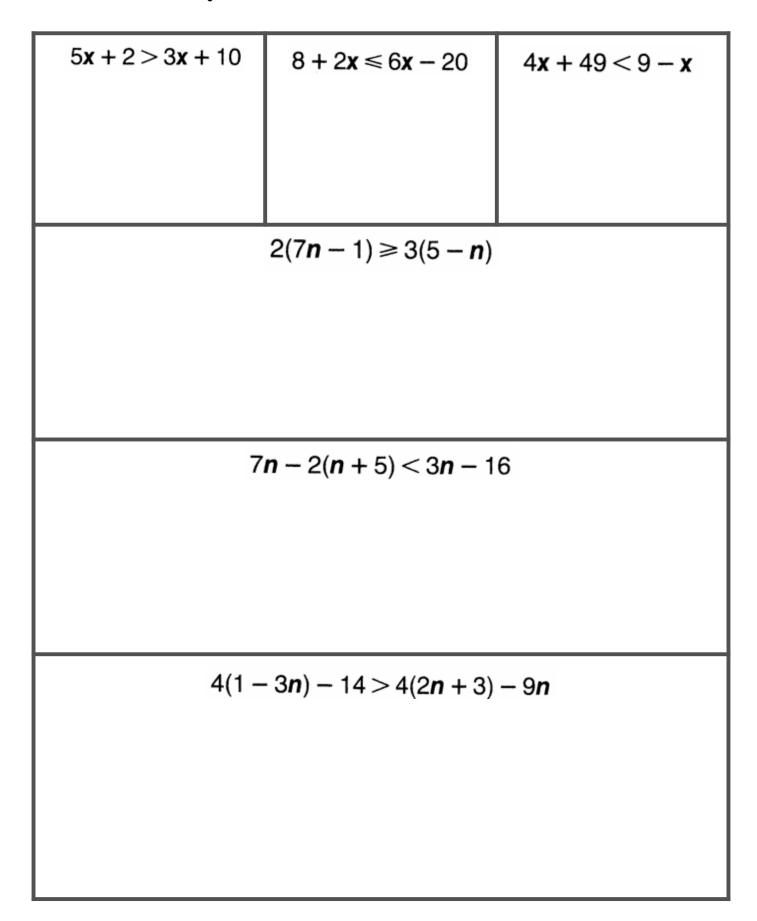
Demo Problems: Solving Inequalities in One Variable

Demo Problems: Solving Inequalities in One Variable

A) $7 + \frac{x}{3} \ge 10$	T) 8x + 6 > 142
U) $-8 + \frac{x}{-6} \ge -9$	E) $-2 + \frac{x}{9} > -1$

Writing and Solving Multi-Step Inequalities in One Variable

$-7x + 4 \ge 18$	$-10 + \frac{x}{3} > -12$		
Canyu Canoe Co. rents canoes for \$8 plus \$3 per hour or any part of an hour. For how many hours can you rent a canoe if you want to spend no more than \$25?			
The Mega Middle School Carniva plus \$0.75 for each ride ticket. buy if you want to spend at mos	How many ride tickets can you		



Name

Date_____

1) In the inequality below, *h* represents the maximum number of hours a family can rent a moving truck while staying within their budget of \$300.

$$20h + 100 \le 300$$

What is *h*, the maximum number of hours the family can rent the truck while staying within their budget?

A.5B.10C.15D.20

2) A monthly phone bill consists of a fixed monthly fee of \$19 and a charge of \$0.25 per minute of use. Which of the following equations can be used to determine the total monthly bill, *t*, for m minutes of use?

A. t = 0.25m + 19B. t = 0.25m - 19C. t = 19m + 0.25D. t = 19m - 0.25

3) Bobby has \$250 in his bank account. He withdraws \$25 each week. How many weeks can he withdraw funds, yet keep at least \$100 in his bank account? Write and solve an inequality to represent this situation. Let *w* represent the number of weeks in your inequality.

- 4) A company packages barbeque sauce in two different-sized bottles, small and large. Although the label on each small bottle states that the bottle contains 18 ounces of sauce, the company allows a tolerance of plus or minus 0.25 ounce for the amount of sauce in each small bottle. In manufacturing, tolerance is the amount of error that is allowed in packaging a product.
 - a. What is the maximum amount of sauce, in ounces, the company allows in each small bottle? Show or explain how you got your answer.

In the absolute-value inequality below, *x* represents the amount of sauce, in ounces, the company allows in each small bottle.

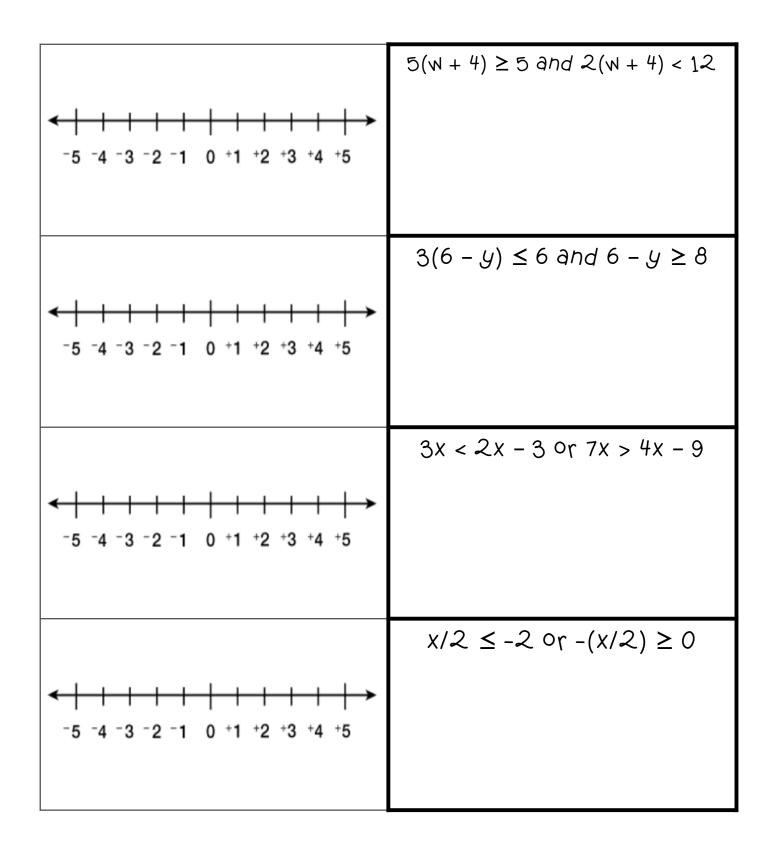
$$|x - 18| \le 0.25$$

b. Solve the absolute-value inequality. Show or explain how you got your answer.

The company also makes a large bottle of barbeque sauce.

- The label on the large bottle states that each bottle contains 24 ounces of sauce.
- The minimum amount of sauce allowed in each large bottle is 23.55 ounces.
- The maximum amount of sauce allowed in each large bottle is 24.45 ounces.
- c. What is the tolerance, in ounces, the company allows for the large bottle? Show or explain how you got your answer.
- d. Write an absolute-value inequality that represents *y*, the amount of sauce, in ounces, the company allows in the large bottle.

Compound Inequalities



D. x+2 = 7	R. 2x + 1 = 7	A. 7 = x
H. x - 3 = 5	E2 7x = -14	R. 2x - 3 - 4 = 3

Things to Remember!



Absolute Value Equations Scavenger Hunt TAKE A VACATION

x = 5		
-5, 5	-5	5
Μ	N	р

-2 x = -12		
No Solution	-6	6, -6
В	0	A

Absolute Value Equations Scavenger Hunt TAKE A VACATION

4 - x = 10		
No Solution	-6	6, -6
I	Н	0

3 x – 2 = 15		
-5, 5	7, –7	7, –3
L	J	N

Absolute Value Equations Scavenger Hunt TAKE A VACATION

x - 2 > 0		
x = 2	-2, 2	All Real Numbers
N	Т	E

$\begin{array}{c c} + & + \\ + & + \\ -4 & -2 & 0 & 2 \end{array}$	x + 1 > 3	$43 \le g \le 49$	$ g-46 \leq 3$
$\leq 4 \mid \emptyset$, the empty set	$ x + 6 \le 4$	identity	<i>x</i> + 6 > 1
	$ x-5 \leq 3$	+ + + + + + + + + + + + + + + + + + +	-2 x < -6
<i>x</i> > 8 OR <i>x</i> < -8.	$\frac{ x }{4} > 2$	$x \ge -2.4$ AND $x \le 2.4$	$ x + 7.4 \le 9.8$ $x \ge -2.4$ AND $x \le 2.4$
<i>x</i> > 7 OR <i>x</i> < -7	x > 7	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	x < 4

Card Sort: Absolute Value Inequality

1-6

Study Guide and Intervention (continued)

Solving Compound and Absolute Value Inequalities

Absolute Value Inequalities Use the definition of absolute value to rewrite an absolute value inequality as a compound inequality.

For all real numbers *a* and *b*, b > 0, the following statements are true.

1. If |a| < b, then -b < a < b.

2. If |a| > b, then a > b or a < -b.

These statements are also true for \leq and \geq .

Example 1 Solve |x+2| > 4. Graph the solution set on a number line.

By statement 2 above, if |x + 2| > 4, then x + 2 > 4 or x + 2 < -4. Subtracting 2 from both sides of each inequality gives x > 2 or x < -6.

-8-6-4-202468

Example 2 Solve |2x - 1| < 5. Graph the solution set on a number line.

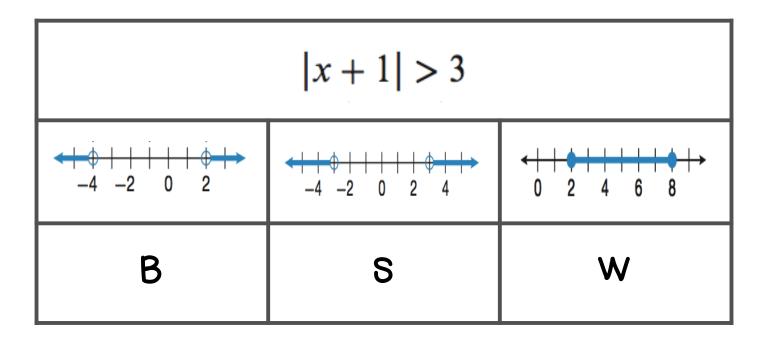
By statement 1 above, if |2x - 1| < 5, then -5 < 2x - 1 < 5. Adding 1 to all three parts of the inequality gives -4 < 2x < 6. Dividing by 2 gives -2 < x < 3. -8-6-4-202468

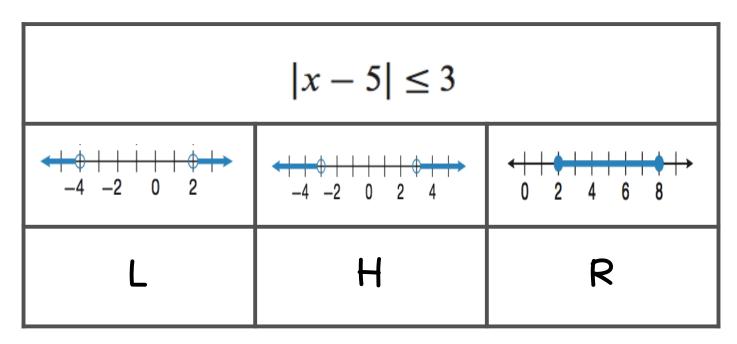
Exercises

Solve each inequality. Graph the solution set on a number line.

1. |3x + 4| < 8**2.** |4s| + 1 > 27-5 -4 -3 -2 -1 0 1 2 3 -8-6-4-202468 **3.** $\left|\frac{c}{2} - 3\right| \le 5$ 4. $|a + 9| \ge 30$ -8 -4 0 4 8 12 16 20 24 -40 -20 0 20 5. |2f - 11| > 96. |5w + 2| < 28-8 -6 -4 -2 0 2 4 6 8 4 - 2 0 2 4 6 8 10 12 8. $\left|\frac{x}{2}-5\right|+2>10$ 7. |10 - 2k| < 2-10 -5 0 5 10 15 20 25 30 2 3 4 5 6 7 8 **9.** |4b - 11| < 1710. |100 - 3m| > 20-4-2024681012 0 5 10 15 20 25 30 35 40

Copyright @ Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc Absolute Value Equations and Inequality Scavenger Hunt "Famous Football Player"





Absolute Value Equations and Inequality Scavenger Hunt "Famous Football Player"

$ x + 6 \le 4$		
Ø, the empty set	x ≤ -2 or x ≥ 2	identity
A	E	I

$$| x - 2 | = 12$$

x = 12 or x = -12 x = 14 or x = -10 x = 10 or x = -14
C D F

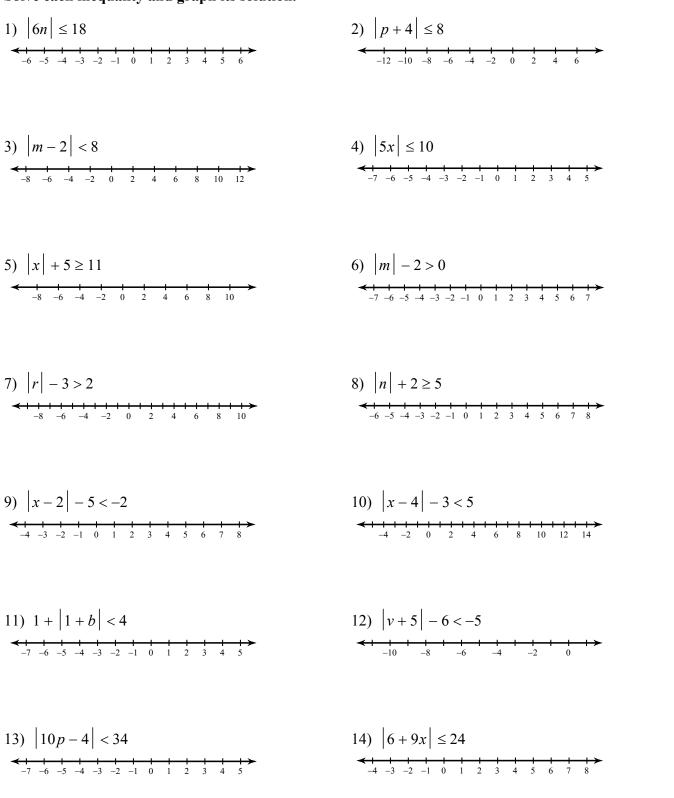
Absolute Value Equations and Inequality Scavenger Hunt "Famous Football Player"

5 - x - 2 = 0		
x = 7	No Solution	x = 7 or x = -3
Μ	κ	Y

Kuta Software - Infinite Algebra 2

Absolute Value Inequalities

Solve each inequality and graph its solution.



Name

Date_____ Period___

17)
$$9 | m - 8 | - 10 < 26$$

$$\begin{array}{c|c} 18) 9 | x + 8 | + 10 < 55 \\ \hline \\ -16 & -14 & -12 & -10 & -8 & -6 & -4 & -2 \end{array}$$

$$19) 9 | r - 2 | -10 < -73$$

20)
$$7 \left| \frac{n}{3} \right| - 9 < 12$$

21)
$$2 | 10b + 7 | -1 > 73$$

$$22) 7 + |6v + 7| \le 60$$

$$(-12) -8 -4 -4 -0 -4 -8 + 8$$

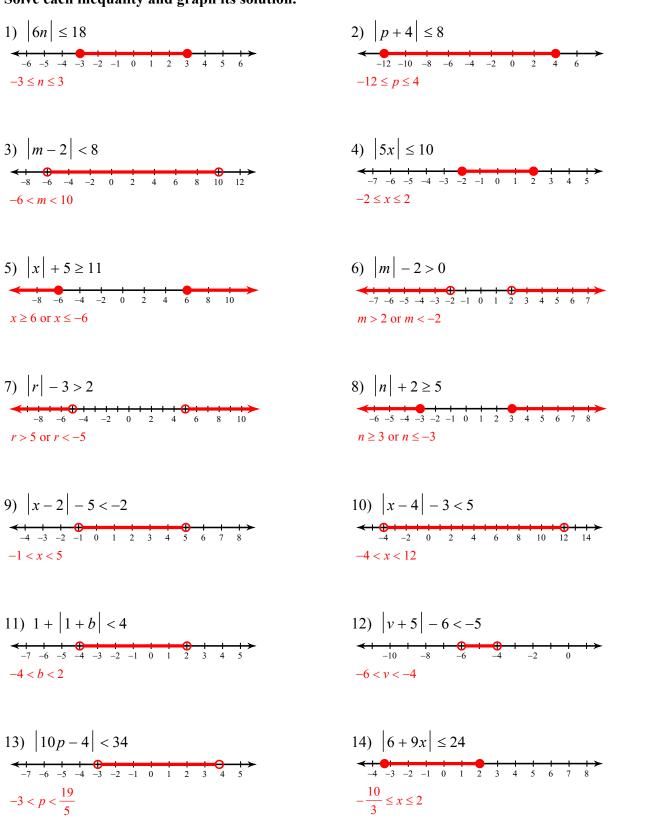
24)
$$9|3n-2|+6>51$$

$$25) \ 3+4 | 3x+7 | \ge -89$$

$$\underbrace{26) \ 9 | 1+8n | -3 \ge 78}_{-5 \ -4 \ -3 \ -2 \ -1 \ 0 \ 1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7}$$

Absolute Value Inequalities

Solve each inequality and graph its solution.



Name

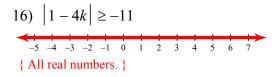
Date_____ Period___

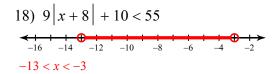
15)
$$|-8a-3| > 11$$

 $-5 -4 -3 -2 -1 = 0$
 $a < -\frac{7}{4}$ or $a > 1$

17)
$$9 | m - 8 | - 10 < 26$$

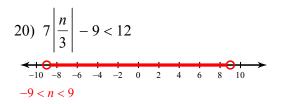
 $4 < m < 12$





19)
$$9|r-2|-10 < -73$$

 $-6 -5 -4 -3 -2 -1 0 1 2 3 4 5 6 7 8$
No solution.



21)
$$2 | 10b + 7 | -1 > 73$$

 $-7 -6 -5 -4 -3 -2 -1 0 1 2 3 4 5 6$
 $b > 3 \text{ or } b < -\frac{22}{5}$

22)
$$7 + |6v + 7| \le 60$$

 $-10 \le v \le \frac{23}{3}$

23)
$$4 | 6 - 2a | + 8 \le 24$$

 $4 | 6 - 2a | + 8 \le 24$
 $4 | 6 - 2a | + 8 \le 24$
 $4 | 6 - 2a | + 8 \le 24$
 $4 | 6 - 2a | + 8 \le 24$
 $4 | 6 - 2a | + 8 \le 24$
 $4 | 6 - 2a | + 8 \le 24$

24)
$$9|3n-2|+6 > 51$$

 $-6 -5 -4 -3 -2 -1 0 1 2 3 4 5 6$
 $n > \frac{7}{3}$ or $n < -1$

25)
$$3 + 4 | 3x + 7 | \ge -89$$

 $\xrightarrow{-6 -5 -4 -3 -2 -1 \ 0 \ 1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7}$
(All real numbers. }
26) $9 | 1 + 8n | -3 \ge 78$
 $\xrightarrow{-5 -4 -3 -2 -1 \ 0 \ 1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7}$
 $n \ge 1 \text{ or } n \le -\frac{5}{4}$

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-8a-3 > 11	$\left 1-4k\right \ge -11$
9 m-8 -10<26	9 x+8 +10 < 55

n + 12 = -7	27 = m + 10
160 = -10x	2n+11 = -13
n + 1.25 = 5.3	0.5n + 1.2 = 3.7
-5(x-2) + 30 = 60	45 = 30 - 3(x + 3)
-50 + 10x = -20(x+3)	<i>x</i> < –10
<i>x</i> – 15 < –18	-10 > <i>n</i> + 16
x - 20 < -18 or $-3x < -21$	x - 2 < 3 and $2x > -10$

2x = 16	3 x-5 = 21	5(x-2)+25 < -50
-90 > -3(5x + 20)	-28 - 6x > -3x + 2	4(x-2) > -3x+6
-6x > -30x + 8 or -2x < -14	-8x > 4 and x - 15 > -11	2x < 14
5 + 3x > 17	3x - 12 = 18	5 x-2 -12=8
3 x-1 +17 < 21	$\frac{ x-1 +3}{4} > 2$	

-28-6x > -3x+24(x-2) > -3x+6t6x t6x 4x-8>-3x+6 -28 > 3x + 27x > 14 $x > 2 \setminus$ $-\frac{30}{3}$ > $\frac{3x}{3}$ -10 > x / x < -103|x-5| = 21|2x| = 16|x-5| = 7 $2\chi = 16$ 2x = -16 $\chi - 5 = 7$ $\chi = 5 = -7$ $\chi = 12$ $\chi = -2$ x = 8 $\chi = -8$ -8 8 -2 12 |2x| < 145 + |3x| > 17 $|3\kappa| > |2$ 2×214 and 2×>-14 $x \ge 7$ $x \ge -7$ barbeils 3x 2-12 3×>12 ar $\times 2 - 4$ X>4 -7 -4 Đ

3|x-1|+17 < 21 $\frac{|x-1|+3}{4} > 2$ 3 x-1 24 |x-1| 2 4/3 x-1243 and x-1>-4 3 12-11+378 |x-1|>5 X-125 or X-16-5 X人王 X>-」 x > 6x 2 - 4 -4 6 - Y3 7/3 |3x| - 12 = 185|x-2|-12=8|3x| = 405|x-2| = 20|x-2| = 43x = 40 ar 3x = -40x=49 x=-49 -40/3 40/3 -2 6 -8x > 4 and x - 15 > -11-6x > -30x + 8 or -2x < -14 $\begin{array}{cccc} 4x > 8 & \overline{-2} & -2 \\ x > \frac{1}{3} & 0 & x > 7 \end{array}$ +15 +15 24x>8 x 4 - 12 and x > 4 barbells Solution No solution! Barbells are not possible

5(x-2)+25 < -50-90 > -3(5x + 20)5x-10+252-50 5x+152-50 -90 > -15x - 60+60 +60 $\frac{5 \times 2 - 65}{\times 2 - 13}$ $\frac{-30}{-15} \xrightarrow{-15}_{-15}$ $22 \times \times \times 2$

Unit 1, Review Problems – Page #1:

Solve each equation. Check your solution. Show your work! 1) x + 23 = 9 2) 18 - x = 24

Solve each equation. Check your solution. Show your work! 3) 7x = -63 4) -8x = 96

Solve each equation. Check your solution. Show your work!

5)
$$3(2x-1) = 21$$
 6) $4(3x+2) = -4$

7)
$$2(5x + 1) = 4(3x - 1)$$

8) $6(x - 6) = 9(2x - 3)$

Solve each equation. Check your solution. Show your work!

9)
$$1.1x - 1.0 = 2.2x - 3.2$$
 10) $\frac{3}{4}x + 6 = \frac{1}{2}x + 3$

Solve each inequality. Then, graph its solution set on the given number line.

11) x + 7 < -2 12) $x - 9 \ge 4$

13)
$$-8 < x + 3$$
 14) $\frac{3}{5}x > -9$

Unit 1, Review Problems – Page #2:

Solve each inequality and graph the solution set. Show your work!

15)	6x – 9 > 33	16)	4x + 3x - 7 < -28
17)	$3(4x-4) \ge 2(5x-4)$	18)	6(3x-4) < 21(x-1)

Solve each inequality. Graph the solution set.

19)	4x – 3 < 5 or 7x + 6 ≥ 41	20)	$8x + 4 \le 4$ or $2x - 16 > -6$
10,		L0)	

Solve each inequality. Graph the solution set.

21)	<i>–</i> 5 < 2x + 9 ≤ 13	22)	–24 ≤ –5x + 11 ≤ –9

Graph each absolute value equation. Graph the solution set.

33) |5x - 8| = 27 34) |7x - 19| + 4 = 13

Graph each absolute value inequality. Graph the solution set.

35) |9x-6| > 12 36) $|3x+3| - 8 \ge 10$

Graph each absolute value inequality. Graph the solution set.

37) $|3x - 4| \le 17$ 38) |7x + 3| - 11 < 20

Unit 1, Review Problems – Page #1:

Solve each equation. Check your solution. Show your work!

1)
$$x + 23 = 9$$

 $\chi = -14$
2) $18 - x = 24$
2) $18 - x = 24$
2) $-6 = \chi$

17=-6

6(x-6) = 9(2x-3)

>-9

Solve each equation. Check your solution. Show your work!

3)
$$7x = -63$$

 $7 = -9$
 $7 = -9$
4) $-8x = 96$

Solve each equation. Check your solution. Show your work!

5)
$$3(2x-1) = 21$$

 $2x = 8$
 $2x - 1 = 7$
 $x = 4$
6) $4(3x + 2) = -4$

7)
$$2(5x+1) = 4(3x-1)$$

 $10x + 2 = 12x - 4$
 $3 = x$
 $3 = x$
 $3 = x$

Solve each equation. Check your solution. Show your work!

9)
$$1.1x - 1.0 = 2.2x - 3.2$$

 $10) \frac{3}{4}x + 6 = \frac{1}{2}x + 3$
 $10) \frac{3}{4}x + 6 = \frac{1}{2}x + 3$
 $10) \frac{3}{4}x + 6 = \frac{1}{2}x + 3$
 $22 = 11x \rightarrow 2 = x$

Solve each inequality. Then, graph its solution set on the given number line.

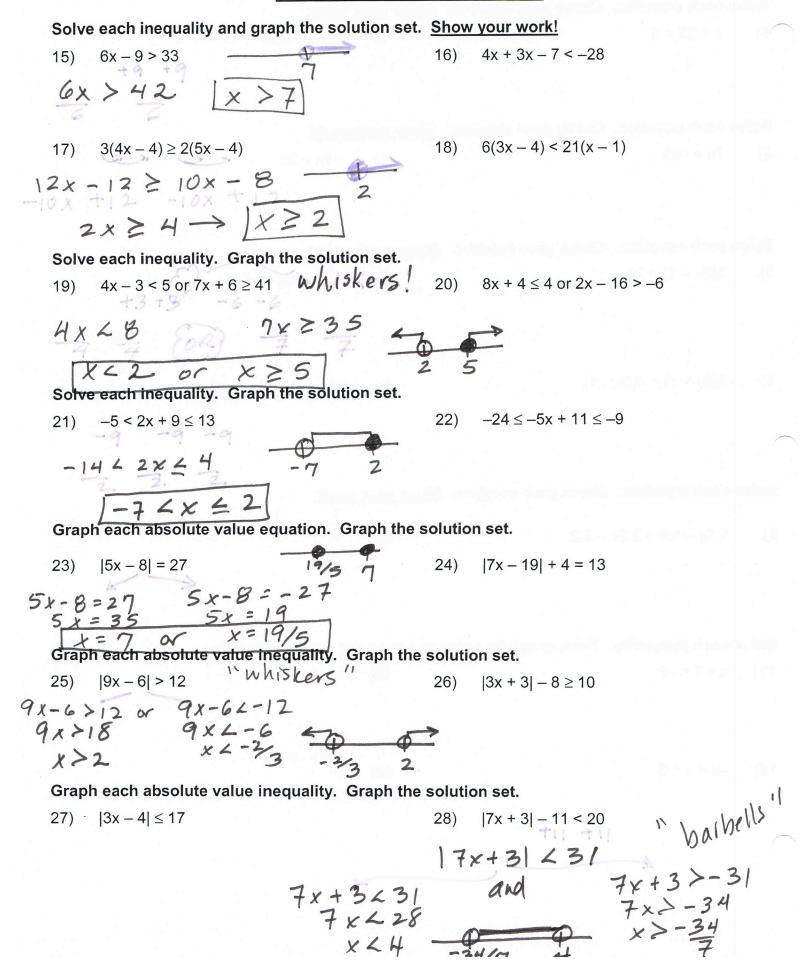
11)
$$x + 7 < -2$$

 $x < -9$
12) $x - 9 \ge 4$
13) $-8 < x + 3$
 $-11 \land \checkmark$
14) $\frac{3}{5}x > -9$

- 11

x > -11

Unit 1, Review Problems - Page #2:



Algebra 1: Unit 1 Assessment Topics EQUATIONS AND INEQUALITIES IN ONE VARIABLE

L19: 1 step equations (+ or -)	L21: 1 step equations (x or ÷)	L23: Solving 2-step equations
L24: Solving decimal equations	L26: Multi Step Equations	L28: Variables on both sides
L50: Graphing Inequalities	L66: Solving Inequalities (+,-)	L70: Solving Inequalities (x,÷)

L73: Compound inequalities	L74: Absolute value equations	L77: Solving multi-step ineqs
L81: Solving Inequalities, variables	L82: Solving compound ineqs	L91: Solve abs value ineq
on both sides		
L94: Multi step abs val eqns	L101: Multi step abs val ineqs	
L94. Multi step abs val equis	LIOI. Multi step abs val megs	